

FIITJEE MONTHLY ASSESSMENT TEST

BATCHES – 1719

CM TEST-3

ANSWER KEY

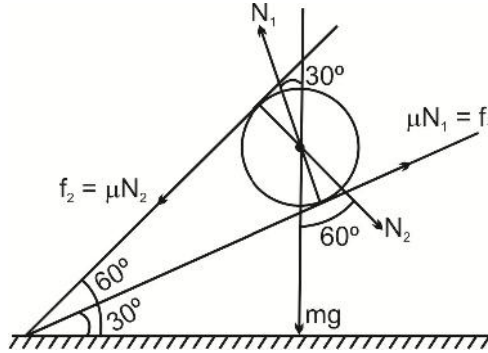
PHYSICS			CHEMISTRY			MATHEMATICS		
Q. No.	Ans.	Concept Code	Q. No.	Ans.	Concept Code	Q. No.	Ans.	Concept Code
1.	A	P111802	1.	C	C110402	1.	B	M110105
2.	A	P111802	2.	B	C110402	2.	D	M110109
3.	D	P111822	3.	D	C110402	3.	C	M112403
4.	B	P111816, P111825	4.	A	C110504	4.	B	M112403
5.	C	P111823	5.	A	C110503	5.	C	M111008
6.	ABC	P111825	6.	AC	C110403	6.	A	M110117
7.	ACD	P111826	7.	ABC	C110402	7.	BD	M110117
8.	ABCD	P111822, P111825	8.	AB	C110403	8.	ABC	M112403
9.	BC	P111816, P111825	9.	ABCD	C110505	9.	AB	M110112
10.	ACD	P111810, P111812	10.	AD	C110501	10.	ABCD	M110112
11.	C	P111816, P111831	11.	ABD	C110501	11.	BC	M112403
12.	BCD	P111825	12.	ACD	C110402	12.	AB	M111007
13.	ACD	P111825, P111826	13.	BCD	C110402	13.	ABD	M111019
PART-C			PART-C			PART-C		
1.	6	P111821	1.	3	C110504	1.	6	M110102
2.	7	P111828	2.	2	C110504	2.	2	M112403
3.	7	P111816, P111822	3.	5	C110506	3.	2	M111007
4.	7	P111825, P111826	4.	5	C110402	4.	3	M110109
5.	2	P111802	5.	4	C110402	5.	7	M111002

Hint and Solution

PHYSICS

Part-A

1. For horizontal equilibrium of sphere
 $N_1 \sin 30^\circ + \mu N_2 \cos 60^\circ = \mu N_1 \cos 30^\circ + N_2 \sin 60^\circ$
 $\frac{N_1}{N_2} = \frac{1}{\sqrt{3}}(4 + \sqrt{3})$



$$\frac{f_1}{f_2} = \frac{\mu N_1}{\mu N_2} = \frac{4}{\sqrt{3}} + 1$$

2. $\tau_0 = 0 \Rightarrow f_2 R = TR$

$$T = 2f \quad \dots (1)$$

$$\text{and } T = f + Mg \sin \alpha \quad \dots (2)$$

$$T = mg \quad \dots (3)$$

$$T = \frac{T}{2} + Mg \sin \alpha$$

$$m = 2 M \sin \alpha$$

3. $I_1 \omega_1 = I_2 \omega_2$

$$\frac{m_0 r^2}{2} \omega_0 = \left[\frac{m_0 r^2}{2} + \mu r^2 \right] \frac{\omega_0}{2}$$

$$m_0 = \frac{m_0}{2} + \mu t$$

$$\mu t = \frac{m_0}{2} \Rightarrow t = \frac{m_0}{2\mu}$$

4. come at heigest pt and point B

$$\frac{1}{2} m (\sqrt{gR})^2 + mg2R = \frac{1}{2} m v_B^2 + MgR$$

$$\frac{1}{2} m v_B^2 = \frac{3}{2} mgR$$

Between A and B

$$mgh = mgR + \frac{1}{2} m v_B^2 + \frac{1}{2} \left(\frac{2}{5} m r^2 \right) \left(\frac{v_B}{r} \right)^2$$

$$mgh = mgR + \frac{3}{2} mgR \left(\frac{7}{5} \right)$$

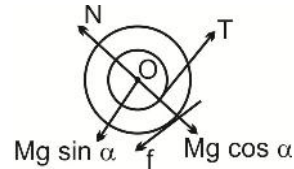
$$h = R + \frac{3}{2} \times \frac{7R}{5} = 3.1R$$

5. $\frac{dL}{dt} = \tau = (r+R)F = (r+R)2t$

$$\int dL = \int (r+R)2t dt$$

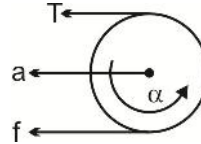
$$L = (r+R)t^2$$

6. $T + f = m_A a \quad \dots (1)$



$$TR - fR = \frac{m_A R^2}{2} \alpha$$

$$T - f = \frac{m_A R}{2} \alpha \quad \dots\dots (2)$$



$$a + R\alpha = 6$$

$$\frac{R\alpha - a = 2}{2R\alpha = 8}$$

$$\alpha = \frac{4}{R} = \frac{4}{4} = 1 \text{ rad/s}^2$$

$$a + 4 = 6 \Rightarrow a = 2 \text{ m/s}^2$$

$$T + f = m_A(2)$$

$$T - f = \frac{m_A(4)}{2} (1)$$

$$2T = 4m_A$$

$$T = 2m_A \Rightarrow f = 0$$

$$m_B g - T = m_B 6$$

$$T = m_B(10 - 6)$$

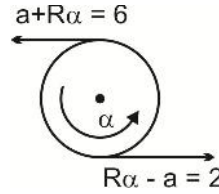
$$T = 2m_A = 4m_B$$

$$\frac{m_A}{m_B} = 2$$

$$l - l_0 = \left(\frac{1}{2} \alpha t^2\right) R$$

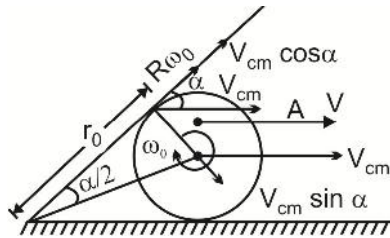
$$= \frac{1}{2} (1) (2)^2 \times 4$$

$$l = l_0 + 8$$



7. $\omega_0 = \frac{V_{cm}}{R} = \frac{V}{R+r}$

$$\omega = \frac{V_{cm} \sin \alpha}{r_0} = \left(\frac{VR}{R+r}\right) \frac{\sin \alpha}{r \cot \frac{\alpha}{2}}$$



$$= \frac{VR}{(R+r)r} \sin \alpha \tan \frac{\alpha}{2}$$

$$S_A = vt$$

$$= v \frac{2\pi}{\omega_0}$$

$$= 2\pi(r+R)$$

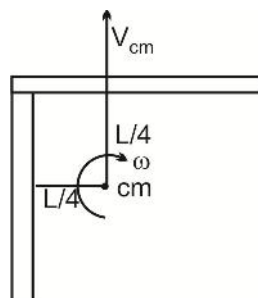
8. $mv_0 = 2mV_{cm}$

COAM about CM

$$mv_0 \frac{L}{4} = 2 \left[\frac{mL^2}{12} + m \left(\frac{L^2}{16} + \frac{L^2}{16} \right) \right] \omega$$

$$L\omega = \frac{V_0 \times 48}{8 \times 10} = \frac{3V_0}{5}$$

$$V_A = \omega \sqrt{\frac{L^2}{16} + \frac{9L^2}{16}} + V_{cm}$$



$$\begin{aligned}
 &= \frac{3v_0}{5} \sqrt{\frac{10}{16}} + \frac{v_0}{2} \\
 &= \frac{v_0}{2} \left[\frac{3}{\sqrt{10}} + 1 \right] \\
 t &= \frac{\theta}{\omega} = \frac{\tan^{-1}(3)}{\omega} \\
 &= \frac{5L}{3V_0} \tan^{-1}(3)
 \end{aligned}$$

9. COME about point A

$$mg \frac{a}{3} \sin \theta = \frac{1}{2} \left[\frac{m(2a)^2}{12} + m \left(\frac{a}{3} \right)^2 \right] \omega^2$$

$$\omega^2 = \frac{3g \sin \theta}{2a}$$

$$f - mg \sin \theta = m \omega^2 \frac{a}{3} = \frac{m 3g \sin \theta a}{3 \cdot 2a} = \frac{mg \sin \theta}{2}$$

$$f = mg \sin \theta + \frac{mg \sin \theta}{2} = \frac{3mg \sin \theta}{2}$$

$$\tau_A = \tau_A \alpha$$

$$mg \frac{a}{3} \cos \theta = \left[\frac{m(2a)^2}{12} + m \left(\frac{a}{3} \right)^2 \right] \alpha$$

$$\alpha = \frac{3g \cos \theta}{4a}$$

$$Mg \cos \theta - N = m \frac{a}{3} \alpha = \frac{mg \cos \theta}{4}$$

$$N = mg \cos \theta - \frac{mg \cos \theta}{4}$$

$$\Rightarrow N = \frac{3mg \cos \theta}{4}$$

$$\mu = \frac{f}{N} = \frac{(3mg \sin \theta) / 2}{(3mg \cos \theta) / 4}$$

$$\Rightarrow \mu = 2 \tan \theta$$

10. (A) $\frac{9MR^2}{2} - \left[\frac{M(R/3)^2}{2} + M \left(\frac{2R}{3} \right)^2 \right]$

$$= \frac{MR^2}{18} [72] = 4MR^2$$

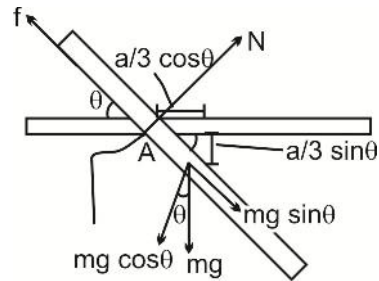
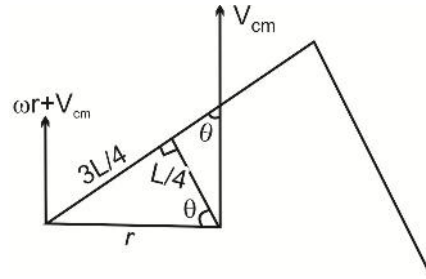
(B) $\frac{9MR^2}{2} + 9M \left(\frac{2R}{3} \right)^2 - \frac{M(R/3)^2}{2}$

$$= \frac{152MR^2}{18}$$

(C) $Y_{cm} = \frac{9M(0) - M \left(\frac{2R}{3} \right)}{9M - M}$

$$= -\frac{2R}{3 \times 8} = -\frac{R}{12}$$

$$\frac{2R}{3} + \frac{R}{12} = \frac{8R + R}{12} = \frac{3R}{4}$$



$$\frac{9MR^2}{2} + 9M\left(\frac{R}{12}\right)^2 - \left[\frac{M\left(\frac{R}{3}\right)^2}{2} + M\left(\frac{3R}{4}\right)^2 \right]$$

$$= \frac{71MR^2}{18}$$

$$(D) \quad 3 \left[\frac{9MR^2}{2} - \frac{M\left(\frac{R}{3}\right)^2}{2} \right]$$

$$= \frac{40}{3}MR^2$$

11. $P = m(u - 0)$

$$P(0.4r) = \frac{2}{5}mr^2(\omega - 0)$$

$$\omega = \frac{P}{mr} = \frac{u}{r}$$

At highest point

$$mv = mv + 4mv$$

$$v = \frac{u}{5}$$

$$KE_{\text{wedge}} = \frac{1}{2}4mv^2$$

$$= \frac{1}{2}4m\left(\frac{u}{5}\right)^2$$

12. $c \sin \theta = b \sin \beta$

$$c \cos \theta \omega_1 = b \cos \beta \omega_2 \quad \dots (1)$$

$$c \cos \theta + b \cos \beta = x$$

$$c \sin \theta \omega_1 + b \sin \beta \omega_2 = v \quad \dots (2)$$

By eq. (1)

$$\omega_1 = \frac{b \cos \beta \omega_2}{c \cos \theta}$$

$$\frac{c \sin \theta b \cos \beta \omega_2}{c \cos \theta} + b \sin \beta \omega_2 = v$$

$$\omega_2 = \frac{v \cos \theta}{b \sin(\theta + \beta)}$$

$$\omega_1 = \frac{b \cos \beta}{c \cos \theta} \times \frac{v \cos \theta}{b \sin(\theta + \beta)}$$

$$\omega_1 = \frac{v \cos \beta}{c \sin(\theta + \beta)}$$

$$= \frac{4v}{15}$$

$$\omega_2 = \frac{v \cos 53^\circ}{4} = \frac{3v}{20}$$

$$V_\theta = c \omega_1 = 3 \left(\frac{4v}{15} \right)$$

$$= \frac{4v}{5}$$

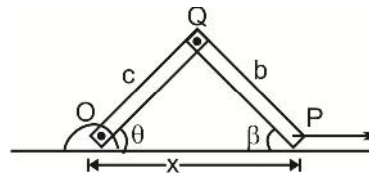
13. $v_c = R\omega = r\omega_c$

$$v_c = 3(4) = 1\omega_c$$

$$\omega_c = 12 \text{ rad/s}$$

$$\alpha = \omega \times \omega_c = (4)(12)$$

$$= 48 \text{ rad/s}^2$$

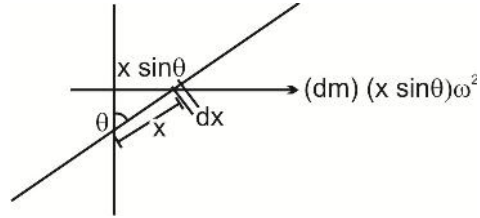


$$KE = \frac{1}{2} m v_{cm}^2 + \frac{1}{2} I \omega_{net}^2$$

$$= 624 \text{ J}$$

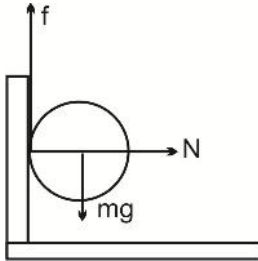
Part – C

1. $dm = (\lambda dx)$
 $d\tau = x \cos \theta dm a_c$
 $= x \cos(\lambda dx)(x \sin \theta)\omega^2$
 $\tau = \int_{-l/2}^{l/2} x^2 \sin \theta \cos \theta \omega^2 \frac{m}{l} dx$
 $= \sin 45^\circ \cos 45^\circ \omega^2 \frac{m}{l} dx$
 $= \frac{\omega^2 m}{2L \times 3} \left[\frac{2L^3}{8} \right]$
 $= \frac{9 \times 4}{6} = 6$



2. $N = ma = \frac{mg}{2}$ (1)

$$fR = \frac{2}{5} mR^2 \alpha$$



$$f = \frac{2}{5} mR\alpha$$
 (2)

$$mg - f = m a_{cm}$$
 (3)

for pure rolling

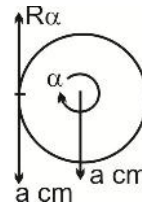
$$a_{cm} = R\alpha$$

$$\frac{mg - f}{m} = R \frac{5f}{2mR}$$

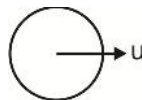
$$f = \frac{2mg}{7} \leq \mu N$$

$$\frac{2mg}{7} \leq \mu \frac{mg}{2}$$

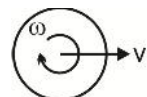
$$\mu \geq \frac{4}{7}$$



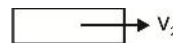
3. $mgh = \frac{1}{2} mu^2$
 $u^2 = 2gh$ (1)
 $V_1 - R\omega = v_2$
 COLM



$$mu = mv_1 + mv_2$$
 (2)
 $v_1 + v_2 = u$
 COAM about cm of shell



$$mu(0) = mv_2R - \frac{2}{3} mR^2 \omega$$



$$v_2 = \frac{2}{3} R\omega$$

by equation (1)

$$v_1 = R\omega + v_2 = \frac{5R\omega}{3}$$

by equation (2)

$$\frac{5R\omega}{3} + \frac{2}{3}R\omega = u$$

$$\omega = \frac{3u}{7R}$$

$$KE_f = \frac{1}{2}mv_1^2 + \frac{1}{2}\left(\frac{2}{3}mR^2\right)\omega^2 + \frac{1}{2}mv_2^2 = \frac{5}{7}mgh$$

$$W_f + Wmg = \Delta KE$$

$$= -\frac{2}{7}mgh$$

4. $r\alpha = a$ (1)

$F - f = ma$ (2)

$Fr = \frac{3}{2}mr^2\alpha$

$F = \frac{3}{2}mr\alpha$

$F = \frac{3}{2}ma$

$F + P = ma_{cm}$

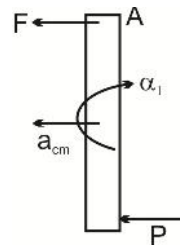
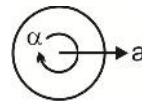
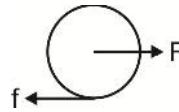
$\frac{PL}{2} - F\frac{L}{2} = \frac{mL^2}{12}\alpha_1$

$\alpha_1 = \frac{6}{mL}(P - F)$

$a_A = \frac{L}{2}\alpha_1 - a_{am} = a$ \Rightarrow

$6P = 14F = 14\left(\frac{3}{2}ma\right)$ \Rightarrow

..... (3)

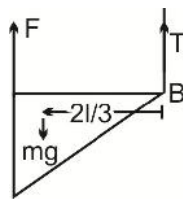


$$\frac{L}{2} \frac{6}{mL} (P - F) - \frac{(F + P)}{m} = \frac{2F}{3m}$$

$$a = \frac{6 \times 2P}{14 \times 3m} = \frac{2P}{7m}$$

5. $\tau_B = 0$

$\Rightarrow mg\frac{2l}{3} - Fl = 0$

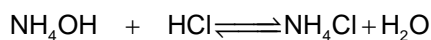
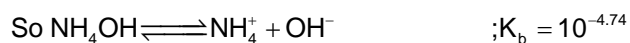
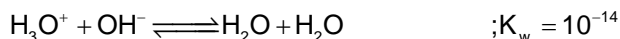
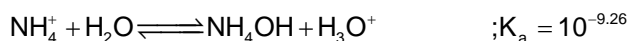


$F = \frac{2mg}{3}$

CHEMISTRY

Part - A

4.



$$300 - x \quad \quad \quad x \text{ mL}$$

$$(300 - x) - x \quad \quad x - x \quad \quad \quad x$$

$$pOH = 14 - pH = pK_b + \log \frac{x}{300 - 2x}$$

$$= 14 - 9.26 = -\log(10^{-4.74}) + \log \frac{x}{300 - 2x}$$

$$\Rightarrow \frac{x}{300 - 2x} = 1$$

$$\Rightarrow 300 = 3x \Rightarrow x = 100 \text{ mL}$$

$$\text{So } v_{\text{NH}_4\text{OH}} : v_{\text{HCl}} :: 2 : 1$$

$$5. \quad pH = \frac{1}{2}[14 - pK_b - \log C]$$

$$2.669 = \frac{1}{2}[14 - pK_b - \log 0.2]$$

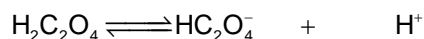
$$pK_b = 14 - 0.3010 - 2 \times 2.669$$

$$-\log K_b = 8.3010 = 8 + 0.3010$$

$$= \log(10^8 \times 2)$$

$$K_b = \frac{1}{2 \times 10^8} = 5 \times 10^{-9}$$

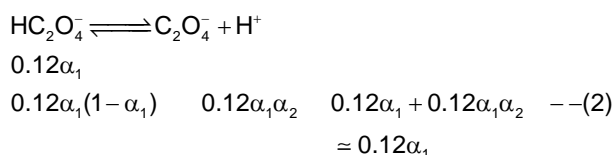
9.



initially 0.12

$$0.12(1 - \alpha_1) \quad \quad 0.12\alpha_1 \quad 0.12\alpha_1 + 0.12\alpha_1\alpha_2 \quad \text{---(1)}$$

$$\approx 0.12\alpha_1$$



$$\text{For (1) } \alpha_1 = \frac{-10^{-2} + \sqrt{(10^{-2})^2 + 4 \times 0.12 \times 0.01}}{2 \times 0.12} = 0.25$$

$$\% \alpha_1 = 25\%$$

$$\text{so } 0.12\alpha_1 = 0.12 \times 0.25 = 0.03$$

$$\text{so } [\text{H}^+] = 0.03$$

$$\text{now } \frac{(0.12\alpha_1)\alpha_2 \times 0.12\alpha_1}{0.12\alpha_1(1-\alpha_2)} = \frac{0.03 \times \alpha_2}{(1-\alpha_2)} = 3 \times 10^{-4}$$

$$= \frac{\alpha_2}{(1-\alpha_2)} = 10^{-2} = \alpha_2 = 10^{-2} \quad 1-\alpha_2 = 1$$

$$\% \alpha_2 = 1\%$$

$$[\text{C}_2\text{O}_4^{2-}] = 0.03 \times 0.01 = 3 \times 10^{-4} \text{M}$$

$$[\text{HC}_2\text{O}_4^-] = 0.03 \times .99 = 0.0297 \text{M}$$

$$[\text{H}_2\text{C}_2\text{O}_4] = 0.12 \times (1-0.25) = 0.09 \text{M}$$

$$10. \quad pOH = -pK_b + \log \frac{[\text{NH}_4\text{Cl}]}{[\text{NH}_4\text{OH}]}$$

$$= -\log(2 \times 10^{-5}) + \log \frac{0.50}{0.25}$$

$$= -\log 2 + 5 + \log 2 = 5$$

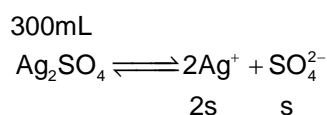
$$\text{So } [\text{OH}^-] = 10^{-5} \text{M}$$

$$\text{Now } [\text{Mg}^{2+}][\text{OH}^-]^2 = 9 \times 10^{-12}$$

$$[\text{Mg}^{2+}] = \frac{9 \times 10^{-12}}{(10^{-5})^2} = 9 \times 10^{-2} \text{M}$$

11. Ag_2SO_4 and PbCrO_4 do not have any common ion so there is no question of precipitation of these two. Now first we have to calculate the conc. of Ag^+ , SO_4^{2-} , Pb^{2+} & CrO_4^{2-} after mixing.

Before mixing:

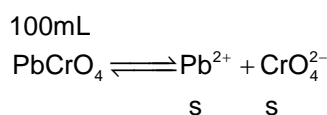


$$4s^3 = 4 \times 10^{-6}$$

$$s = 10^{-2}$$

$$\text{so } [\text{Ag}^+] = 2 \times 10^{-2}$$

$$[\text{SO}_4^{2-}] = 10^{-2}$$



$$s^2 = 16 \times 10^{-14}$$

$$s = 4 \times 10^{-7}$$

$$\text{so } [\text{Pb}^{2+}] = 4 \times 10^{-7}$$

$$[\text{CrO}_4^{2-}] = 4 \times 10^{-7}$$

After mixing:

$$[\text{Ag}^+] = 2 \times 10^{-2} \times \left(\frac{3}{4}\right)$$

$$[\text{Pb}^{2+}] = 4 \times 10^{-7} \times \left(\frac{1}{4}\right)$$

$$[\text{SO}_4^{2-}] = 10^{-2} \times \left(\frac{3}{4}\right)$$

$$[\text{CrO}_4^{2-}] = 4 \times 10^{-7} \times \left(\frac{1}{4}\right)$$

Now Ionic product for $\text{PbSO}_4 =$

$$\left(\frac{4 \times 10^{-7}}{4}\right) \times \left(\frac{10^{-2} \times 3}{4}\right) = 7.5 \times 10^{-10}$$

$$\leq K_{sp}[\text{PbSO}_4]$$

So PbSO_4 will not precipitate out.

Now Ionic product for Ag_2CrO_4 =

$$\left(2 \times 10^{-2} \times \frac{3}{4}\right)^2 \times \left(\frac{4 \times 10^{-7}}{4}\right) = 2.25 \times 10^{-11}$$

$$= 22.5 \times 10^{-12}$$

$$\geq K_{sp}[\text{Ag}_2\text{CrO}_4]$$

So some Ag_2CrO_4 will precipitate out.

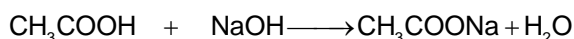
Part C

1.

m.m of $\text{NaOH} = 30 \times 0.2 = 6$ m.m

m.m of $\text{CH}_3\text{COOH} = 50 \times 0.2 = 10$ m.m

Now:



$$\begin{array}{ccc} 10 & 6 & 0 \\ 10 - 6 = 4 & 6 - 6 = 0 & 6 \end{array}$$

$$\text{pH} = -\log(2 \times 10^{-5}) + \log \frac{6}{4}$$

$$= 4.87$$

Suppose 'v' mL of NaOH is added then

m.m of $\text{CH}_3\text{COONa} = (6 + v \times 0.2)$

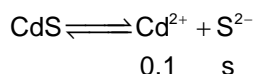
m.m of $\text{CH}_3\text{COOH} = (4 - v \times 0.2)$

$$5 = -\log(2 \times 10^{-5}) + \log \left(\frac{6 + 0.2v}{4 - 0.2v} \right)$$

$$0.3010 = \log \left(\frac{6 + 0.2v}{4 - 0.2v} \right)$$

$$\text{So } \left(\frac{6 + 0.2v}{4 - 0.2v} \right) = 2 \Rightarrow v = 3.33 \text{ mL}$$

2.



For precipitation of CdS

$$[\text{Cd}^{2+}][\text{S}^{2-}] = K_{sp}(\text{CdS})$$

$$0.1 \times [\text{S}^{2-}] = 8 \times 10^{-27}$$

$$[\text{S}^{2-}] = 8 \times 10^{-26}$$

For precipitation of ZnS

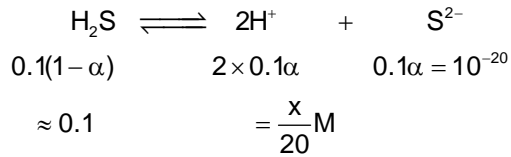
$$[\text{Zn}^{2+}][\text{S}^{2-}] = K_{sp}(\text{ZnS})$$

$$0.1 \times [\text{S}^{2-}] = 10^{-21}$$

$$[\text{S}^{2-}] = 10^{-20}$$

CdS will start precipitate as the conc of $[\text{S}^{2-}] = 8 \times 10^{-26}$ and ZnS will start precipitate as the conc of $[\text{S}^{2-}] = 10^{-20}$ so we can raise the concentration of $[\text{S}^{2-}]$ upto 10^{-20}

Now

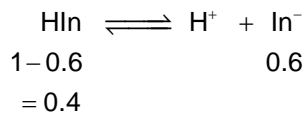


$$\frac{\left(\frac{x}{20}\right)^2 \times 10^{-20}}{0.1} = 10^{-21} \Rightarrow \left(\frac{x}{20}\right)^2 = 10^{-2}$$

$$\frac{x}{20} = 10^{-1}$$

$$x = 2$$

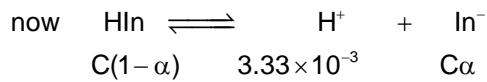
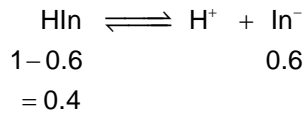
3.



$$\text{pH} = \text{pK}_{\text{In}} + \log \frac{[\text{In}^-]}{[\text{HIn}]}$$

$$2.176 = \text{pK}_{\text{In}} + \log \frac{0.6}{0.4}$$

$$\text{pK}_{\text{In}} = 2 \Rightarrow \text{K}_{\text{In}} = 10^{-2}$$



$$\frac{3.33 \times 10^{-3} \times \text{C}\alpha}{\text{C}(1-\alpha)} = 10^{-2}$$

$$\frac{\alpha}{1-\alpha} = 3 \Rightarrow \alpha = 3 - 3\alpha$$

$$\Rightarrow \alpha = 0.75$$

$$\text{So } [\text{HIn}] = 1 - 0.75 = 0.25$$

$$\%[\text{HIn}] = 25\%$$

Mathematics

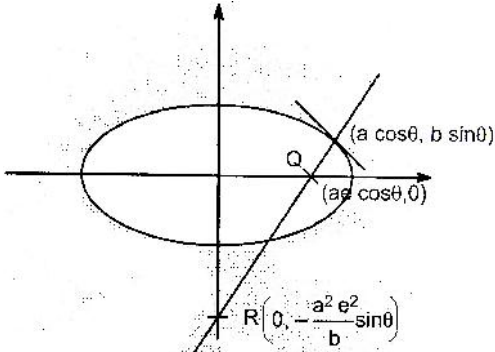
Part – A

5.

C

$$2h = ae^2 \cos\theta$$

$$2k = \frac{-a^2 e^2 \sin\theta}{b}$$



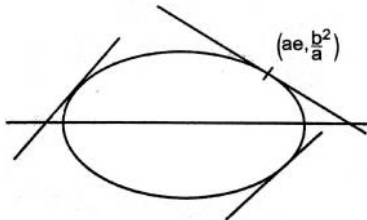
$$\Rightarrow \frac{4h^2}{(ae^2)^2} + \frac{4k^2}{\left(\frac{a^2 e^2}{b}\right)^2} = 1$$

$$\frac{x^2}{\left(\frac{ae^2}{2}\right)^2} + \frac{y^2}{\left(\frac{a^2 e^2}{2b}\right)^2} = 1$$

$$\Rightarrow b^2 = a^2 (1 - e'^2)$$

$$\Rightarrow e = e'$$

12. AB



Tangents at extremities of L.R. are

$$\frac{xe}{a} + \frac{y}{a} = 1$$

or
$$\frac{xe}{a} - \frac{y}{a} = 1$$

$$xe + (y - a) = 0$$

or
$$xe - (y + a) = 0$$

Fixed points are (0, a) or (0, -a)

13. ABD

$$\angle SQP = \angle S'QP = \frac{\pi}{2}$$

⇒ S', Q, S are collinear

T is radical centre of C, C₁ and C₂.

Equation of circle C₂

$$C_2 : (x - a \cos \theta)(x + ae) + (y - b \sin \theta)y = 0$$

$$C : x^2 + y^2 - a^2 = 0$$

Equation of tangent to C₂ and C is

$$a(\cos \theta - e)x + b \sin \theta y + a^2(e \cos \theta - 1) = 0$$

Put $x = a \cos \theta$

$$a^2(\cos^2 \theta - e \cos \theta) + b \sin \theta y + a^2(e \cos \theta - 1) = 0$$

⇒ $b \sin \theta y = a^2 \sin^2 \theta$

$$\Rightarrow y = \frac{a^2}{b} \sin \theta$$

$$y = \left(a \cos \theta, \frac{a^2}{b} \sin \theta \right)$$

Equation of chord of contact of T w.r.t.

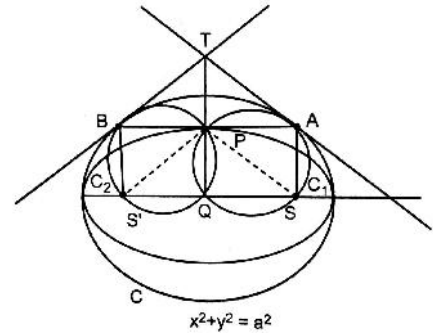
$$x^2 + y^2 = a^2$$

$$x \cos \theta + y \frac{a}{b} \sin \theta = a$$

⇒ $\frac{x \cos \theta}{a} + \frac{y \sin \theta}{b} = 1$ which is same as equation of tangent to ellipse at P.

∴ SA and S'B both are ⊥ to AB

⇒ S'B || SA



Part - C

1. 6
2. 2
3. 2

Equation of tangent to $\frac{x^2}{4} + y^2 = 1$ at point $(2 \cos \theta, \sin \theta)$ is

$$\frac{x \cos \theta}{2} + y \sin \theta = 1 \quad \dots\dots (1)$$

Equation of chord of contact of R(h, k)

$$\text{w.r.t. } \frac{x^2}{6} + \frac{y^2}{3} = 1 \text{ is}$$

$$\frac{hx}{6} + \frac{ky}{3} = 1$$

∴ Eq. (1) and (2) are identical

$$\Rightarrow \frac{h/3}{\cos \theta} = \frac{k/3}{\sin \theta} = 1$$

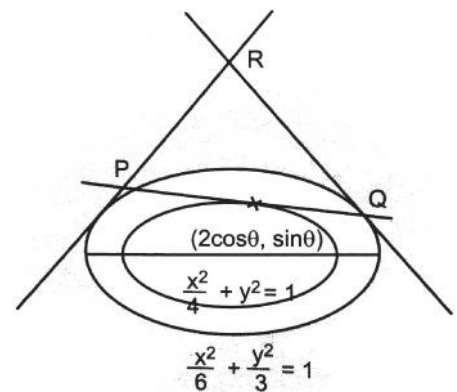
$$\Rightarrow h^2 + k^2 = 9 = 6 + 3$$

⇒ (h, k) lies on director circle of ellipse

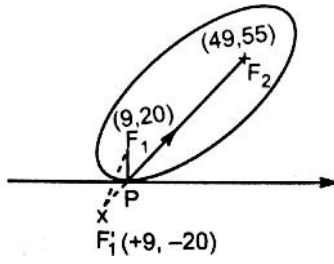
$$\frac{x^2}{6} + \frac{y^2}{3} = 1$$

$$\Rightarrow k = 2$$

4. 3



5. 7



$$2a = PF_1 + PF_2 = PF_1' + PF_2$$

$$= F_1'F_2 = \sqrt{40^2 + (75)^2} = 85$$

$$\Rightarrow L = 85$$

$$\therefore \left[\frac{L}{11} \right] = 7$$