ANSWERKEY																				
Q.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
A.	2	2	2	1	1	2	1	3	4	2	1	4	3	4	1	4	3	1	1	3
Q.	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
A.	2	2	4	3	4	1	4	4	4	4	1	1	3	2	1	3	2	4	1	2
Q.	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
A.	4	1	4	4	4	2	2	3	4	2	1	2	1	2	1	2	3	4	2	4
Q.	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80
A.	3	4	3	4	3	4	3	2	1	4	3	3	3	4	4	2	3	3	4	1
Q.	81	82	83	84	85	86	87	88	89	90										
A.	3	4	4	4	2	1	4	1	3	4										

SOLUTION

- 2. NCERT XIII Part 1 Page 72.
- In fcc unit cell $4r = \sqrt{2}$ a 3. [r = radius of Cu atom, a = edge length]

So,
$$r = \frac{\sqrt{2a}}{4}$$

$$r = \frac{\sqrt{2} \times 361}{4} = 127 \text{ pm}$$

- $Sb_2S_3 \rightarrow 2Sb^{+2} + 3S^{--}_{3x}; K_{sp} = (2x)^2.(3x)^3$ $K_{sp} = 108x^5$; $K_{sp} = 108 \times (1 \times 10^{-5})^5 = 108 \times 10^{-25}$ It is buffer solution so,
- 5.

$$pH = pK_a + log \frac{Salt}{Acid}$$

$$pH = pK_a - log \frac{Acid}{Salt} \left(Given \frac{[Acid]}{[Salt]} = 10:1 \right)$$

$$pH = pK_a - log 10$$

$$pH = pK_a - 1$$

- NCERT-XII, Part-I, Page-48(formula-2.26). 6.
- 7. $P_{B} = p_{B}^{\circ} X_{B}^{\circ}; \therefore P_{B} = \frac{\frac{78}{78}}{\frac{78}{78} + \frac{46}{92}} \times 75; \therefore P_{B} = 50 \text{ torr}$

NCERT XIth Part-I Page No. 142. 8. Let the mass of methane and oxygen is w

mole fraction of oxygen =
$$\frac{\frac{w}{32}}{\frac{w}{32} + \frac{w}{16}}$$

$$= \frac{\frac{1}{32}}{\frac{1}{32} + \frac{1}{16}} = \frac{\frac{1}{32}}{\frac{3}{32}} = \frac{1}{3}$$
 Let the total pressure be P

The pressure exerted by oxygen (partial pressure)

=
$$X_{O_2} \times P_{total} \Rightarrow P \times \frac{1}{3}$$
. Hence (3) is correct.

NCERT XI Part 1 Page # 196

A + B
$$\rightarrow$$
 2C (3-0.75) (1-0.75) 1.5

$$K = \frac{[C]^2}{[A][B]} = \frac{(1.5)^2}{2.25 \times 0.25} = \frac{2.25}{2.25 \times 0.25} = 4.0$$

- NCl₅, PH₅, CuI₂ exist नहीं करते हैं। 23.
- PCl₃ is sp³ hybridised and pyramidal in shape. $PCl_3 sp^3$ संकरण का होता है यह पिरामीडीय होता है।

26. [X] is MnO₄²⁻

$$x + 4 (-2) = -2$$

 $x = + 6$

- **28.** SO_2 , Cl_2O_7 , $N_2O_5 \longrightarrow Acidic$ nature oxides $N_2O \longrightarrow Neutral$ oxide.
- 29. ClO₄[⊙] does not disproportionate because in this oxoanion chlorine is present in its highest oxidation state.
- **30.** $CCl_4 + H_2O \xrightarrow{R.T.}$ No reaction
- **31.** Difference of roots

$$\alpha - \beta = (\alpha + h) - (\beta + h)$$

$$\frac{\sqrt{D_1}}{a} = \frac{\sqrt{D_2}}{p}$$
 $\frac{D_1}{D_2} = \frac{a^2}{p^2}$

32. $a(p + x)^2 + 2bpx + c = 0$ roots are q, r

product of roots = $qr = p^2 + \frac{c}{a}$

- 34. a(bc 1) 1(c 1) + (1 6) > 0 abc - a - b - c + 2 > 0 ...(1) A > G
 - $\frac{a+b+c}{3} > (abc)^{1/3} \implies (a+b+c) -3(abc)^{1/3} > 0 ...(2)$

on adding $eq^n(1)$ and (2)

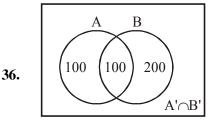
$$abc - 3(abc)^{1/3} + 2 > 0$$

$$x^3 - 3x + 2 > 0$$

$$(x-1)^2 (x+2) > 0$$

$$x > -2$$

$$(abc)^{1/3} > -2 = abc > -8$$



 $n(A' \cap B') = 700 - 400 = 300$

38. Since a, b, c are the roots of the equation $x^3 - 3x^2 + x + \lambda = 0$ \Rightarrow a + b + c = 3 \Rightarrow a + b = 3 - c Now area of the triangle will be

$$A = \frac{1}{2} \times \frac{1}{a+b} \times 1 = \frac{1}{2(a+b)} = \frac{1}{2(3-c)}$$

$$\Rightarrow \frac{dA}{dc} = \frac{1}{2(3-c)^2} > 0$$

As A is an increasing function & $c \in [1,2]$

$$\therefore A_{\text{max}} = \frac{1}{2} \text{ sq. units.}$$

39.
$$\vec{\alpha} \cdot \vec{\beta} = |\vec{\alpha}| |\vec{\beta}| \cos \frac{\pi}{4}$$

$$\sqrt{2}a + 3\sqrt{2}b + 4c = I.6.\frac{1}{\sqrt{2}}$$

$$a + b + 2\sqrt{2} C = I.3$$

$$\Rightarrow$$
 LHS is integer if $c = 0$

then $\vec{\alpha} = a\hat{i} + b\hat{j}$ which lies in xy plane

40. Let P(h, k) be the point from which two tangents are drawn to $y^2 = 4x$. Any tangent to the parabola $y^2 = 4x$ is

$$y = mx + \frac{1}{m}$$

If it passes through P(h, k), then

$$k = mh + \frac{1}{m} \implies m^2 h - mk + 1 = 0$$

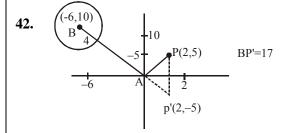
Let m₁, m₂ be the roots of this equation. Then,

$$m_1 + m_2 = \frac{k}{h}$$
 and $m_1 m_2 = \frac{1}{h}$

$$\Rightarrow$$
 3m₂ = $\frac{k}{h}$ and 2m₂² = $\frac{1}{h}$ [: $m_1 = 2m_2$ (given)]

$$\Rightarrow 2\left(\frac{k}{3h}\right)^2 = \frac{1}{h} \Rightarrow 2k^2 = 9h$$

Hence, P(h, k) lies on $2y^2 = 9x$



44.
$$\frac{dy}{dx}\Big|_{(x_1y_1)} = \frac{4x_1}{y_1} = 4 \Rightarrow y_1 = x_1$$

 (x_1, y_1) lies on $4x^2 - y^2 = 12$
 $\Rightarrow x_1 = y_1 = \pm 2$

 \therefore Equation of tangent lines with slope 4 are y = 4x + 6 & y = 4x - 6

$$\Rightarrow |c_1 - c_2| = 12$$

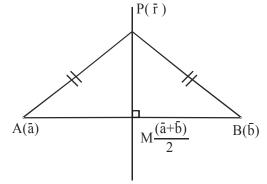
46. Eq of plane O Q R is

$$\begin{vmatrix} x & y & z \\ 1 & 3 & 4 \\ 2 & 1 & -2 \end{vmatrix} = 0$$

$$\Rightarrow$$
 2x - 2y + z = 0

distance of P from plane = $\left| \frac{6+4-1}{\sqrt{4+4+1}} \right| = 3$

47.



$$\overline{\text{MP}} \perp \overline{\text{AB}}$$

$$\Rightarrow \overline{MP} \cdot \overline{AB} = 0$$

$$\Rightarrow \left(\overline{r} - \frac{\overline{a} + \overline{b}}{2}\right) \cdot \left(\overline{b} - \overline{a}\right) = 0$$

$$\Rightarrow \left[\overline{r} - \frac{1}{2} \left(\overline{a} + \overline{b} \right) \right] \left(\overline{a} - \overline{b} \right) = 0$$

49. Statement-2 is clearly true.

Since
$$\overrightarrow{OM} = \lambda \overrightarrow{OD} = \lambda \overrightarrow{d}$$

Now points A, B, C and M are coplanar

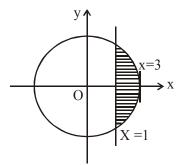
$$\Rightarrow [\vec{a} \ \vec{b} \ \vec{c}] = [\vec{m} \ \vec{a} \ \vec{b}] + [\vec{m} \ \vec{b} \ \vec{c}] + [\vec{m} \ \vec{c} \ \vec{a}]$$
$$= [\lambda \vec{d} \ \vec{a} \ \vec{b}] + [\lambda \vec{d} \ \vec{b} \ \vec{c}] + [\lambda \vec{d} \ \vec{c} \ \vec{a}]$$

$$\Rightarrow \lambda = \frac{[\vec{a} \ \vec{b} \ \vec{c}]}{[\vec{d} \ \vec{a} \ \vec{b}] + [\vec{d} \ \vec{b} \ \vec{c}] + [\vec{d} \ \vec{c} \ \vec{a}]}$$

and therefore Statement-1 is also true.

51. Since the area is symmetrical about x-axis, so

area =
$$2 \int_{1}^{3} \sqrt{9 - x^2} dx$$



$$= \left[x\sqrt{9-x^2} + 9\sin^{-1} x/3 \right]_{1}^{3}$$

$$= 9\pi/2 - \sqrt{8} - 9 \sin^{-1}(1/3)$$

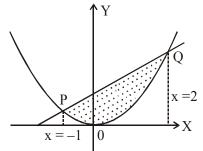
$$= 9 (\pi/2 - \sin^{-1} 1/3) - \sqrt{8} = 9 \sec^{-1} 3 - \sqrt{8}$$

52. Solving the equation of the given curves for x, we get

$$x^2 = x + 2$$

$$\Rightarrow (x-2)(x+1) = 0$$

$$\Rightarrow$$
 x = -1, 2



So reqd. area =
$$\int_{-1}^{2} \left[\frac{x+2}{4} - \frac{x^2}{4} \right] dx$$

$$=\frac{1}{4}\left[\frac{x^2}{2}+2x-\frac{x^3}{3}\right]_{-1}^2$$

$$= \frac{1}{4}[(2+4-8/3)-(1/2-2+1/3)] = \frac{9}{8}$$

53. Given equation can be written as

$$\left\lceil 1 + \left(\frac{d^2y}{dx}\right)^3 \right\rceil^4 = \left(\frac{m}{m+1}\right)^5 \left(\frac{d^3y}{dx^3}\right)^5$$

This shows that its order = 3, degree = 5

54.
$$a = 2\cos\frac{\alpha+\beta}{2}\cos\frac{\alpha-\beta}{2} - 2\cos^2\frac{\alpha+\beta}{2} + 1$$
$$= 2\cos\frac{\alpha+\beta}{2}\left(\cos\frac{\alpha-\beta}{2} - \cos\frac{\alpha+\beta}{2}\right) + 1$$
$$= 2\cos\frac{\alpha+\beta}{2} \cdot 2\sin\frac{\alpha}{2}\sin\frac{\beta}{2} + 1 = b+1$$
$$\Rightarrow a - b = 1$$

55.
$$\sin^2 x \cos^2 x (1 - \sin^2 x) = 1$$

 $\sin^2 x \cos^4 x = 1$
No value of x for L.H.S. = R.H.S.

56. Given,
$$\sigma_{10}^2 = \frac{99}{12} = \frac{33}{4}$$

$$\Rightarrow \sigma_{10} = \frac{\sqrt{33}}{2}$$

SD of required series = $3\sigma_{10} = \frac{3\sqrt{33}}{2}$

57.
$$A \wedge (A \vee B)$$
 is F when $A = F$
 $A \vee (A \wedge B)$ is F when $A = F$, $B = F$
We have

$$[A \land (A \to B)] \to B$$

$$\equiv [A \land (\sim A \lor B)] \to B$$

$$\equiv [(A \land (\sim A)) \lor (A \land B)] \to B$$

$$\equiv A \wedge B \to B$$

$$\equiv \sim (A \wedge B) \vee B$$

$$\equiv [(\sim A) \vee (\sim B)] \vee B$$

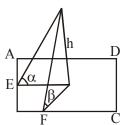
$$\equiv (\sim A) \vee (\sim B) \vee B$$

$$\equiv (\sim A) \vee [(\sim B) \vee B]$$

$$\equiv (A) \lor T \equiv T$$

$$\therefore$$
 [A \land (A \rightarrow B)] \rightarrow B is a tautology.

58.



Statement-2 is True. In statement-1 if the height of the pole is h, then the length of the adjacent sides of the field are 2h cot α and 2h cot β and the area if $4h^2$ cot α cot $\beta = 4h^2$ as $\alpha + \beta = \pi/2$ \Rightarrow cot α cot $\beta = 1$.

So
$$4h^2 = 2500 \Rightarrow h = 25$$
 units.

and the statement-1 is true using statement-2.

59.
$$f(x) = x^3 - x^2 + 100x + 1001$$

 $f'(x) = 3x^2 - 2x + 100 > 0$ ∀ × ∈ R
∴ $f(x)$ is increasing (strictly)

$$\therefore f\left(\frac{1}{1999}\right) > f\left(\frac{1}{2000}\right)$$
$$f(x+1) > f(x-1)$$

60. Let
$$f(x) = x^2 \ln \frac{1}{x} = -x^2 \ln x$$

$$\therefore f'(x) = -2x \, \ell n \, x - x = 0 \quad \Rightarrow \quad x = e^{-1/2}$$

$$\lim_{x \to 0} f(x) = 0, \ \lim_{x \to \infty} f(x) = -\infty \text{ and } f(e^{-\frac{1}{2}}) = \frac{1}{2e}$$

 \therefore Maximum value of f(x) is $\frac{1}{2e}$

61.
$$X = \frac{A^2B}{C^{1/3}D}$$

$$\frac{\Delta X}{X} = 2\frac{\Delta A}{A} + \frac{\Delta B}{B} - \frac{1}{3}\frac{\Delta C}{C} - \frac{\Delta D}{D}$$

$$=2\times2\%+2\%-\frac{1}{3}\times4\%-5\%$$

$$=4\%+2\%-\frac{4}{3}\%-5\%$$

The percentage error contributed by C is $\frac{4}{3}$ which is minimum among A, B, C and D.

62. (i)
$$[(a\cos\theta)\hat{i} + (b\sin\theta)\hat{j}]$$
. $[(b\sin\theta)\hat{i} - (a\cos\theta)\hat{j}]$
= $ab\sin\theta\cos\theta - ba\sin\theta\cos\theta = 0$

(ii) $[a(\cos \theta)\hat{i} + (b \sin \theta)\hat{j}].$

$$\left[\left(\frac{1}{a} \sin \theta \right) \hat{i} - \left(\frac{1}{a} \cos \theta \right) \hat{j} \right]$$

$$= \sin \theta \cos \theta - \sin \theta \cos \theta = 0$$

(iii) [(a cos
$$\theta$$
) \hat{i} + (b sin θ) \hat{j}]. $5\hat{k} = 0$

Hence, all the three options are correct because the dot product of two perpendicular vectors is zero. 63. Using $v^2 = u^2 - 2gh$ (for vertically upward motion under gravity)

$$0 = u^2 - 2 \times 10 \times 5$$

 $u = 10 \text{ ms}^{-1}$

Also using u = u - gt

$$0 = 10 - 10 \times t$$
 $t = 1s$

which means the each ball is thrown after 1 sec. Therefore the number of balls thrown up per minute is 60.

64. Velocity of the stone relative to the ground = 10 + 5 = 15 m/s (upwards)

Velocity of the stone after 2s, relative to the ground

$$v = 15 - 10 \times 2 \quad (using, v = u - gt)$$

$$v = -5 \text{ ms}^{-1}$$

or
$$|v| = +5 \text{ ms}^{-1}$$

65. Given $x = ct + bt^2 - ct^3$

velocity
$$v = \frac{dx}{dt} = a + 2bt - 3ct^2$$

and acceleration
$$f = \frac{dv}{dt} = 2b - 6ct$$

Acceleration is zero at time

$$2b - 6ct = 0$$
 $t = \frac{b}{3c}$

Putting this value of t in eq. (i), we get

$$v = a + 2b \left(\frac{b}{3c}\right) - 3c \left(\frac{b}{3c}\right)^2$$

or
$$v = a + \frac{2b^2}{3c} - \frac{b^2}{3c} = a + \frac{b^2}{3c}$$

66. Given, $R = 4\sqrt{3} H$

$$\frac{\mathrm{u}^2 \sin 2\theta}{\mathrm{g}} = \frac{4\sqrt{3}\mathrm{u}^2 \sin^2 \theta}{2\mathrm{g}}$$

or
$$2 \sin \theta \cos \theta = 2\sqrt{3} \sin^2 \theta$$

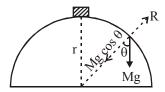
or
$$\cos \theta = \sqrt{3} \sin \theta$$

$$\tan \theta = \frac{1}{\sqrt{3}} \implies \theta = 30^{\circ}$$

67. $\operatorname{Mg} \cos \theta - R = \frac{\operatorname{Mv}^2}{r}$

when the body leaves the surface, R = 0

$$Mg\cos\theta = \frac{Mv^2}{r}$$



$$\cos\theta = \frac{v^2}{rg} = \frac{(5)^2}{5 \times 10} = \frac{1}{2}$$

$$\theta = 60^{\circ}$$

68. Time taken to reach the bag on the ground

$$t = \sqrt{\frac{2h}{g}} = \sqrt{\frac{2 \times 490}{9.8}} = 10s$$

 \therefore R = 150 × 10 = 1500m

69.
$$H_{\text{max}} = \frac{u^2 \sin^2 \theta}{2g} = 4$$

$$R = \frac{u^2 \sin^2 2\theta}{g} = 12$$

Dividing both the equations, we get

$$\tan \theta = \frac{4}{3}$$
 or $\sin \theta = \frac{4}{5}$

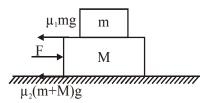
Putting the value of $\sin \theta$ in eqn. (i), we get,

$$u^2 = \frac{8g}{16/25}$$

or

$$u = 5\sqrt{g/2}$$

70.
$$F = \mu_2 (m + M) g + (M + m)a$$
(i)



Now, since the friction force between m and M is μ_1 mg, the acceleration.

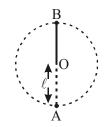
$$a = \frac{Force}{mass} = \frac{\mu_1 mg}{m} = \mu_1 g$$

Putting the value of a in eqn. (i), we get

$$F = \mu_2(m + M)g + \mu_1(m + M)g$$

= $(\mu_1 + \mu_2) (m + M)g$
= $(0.5 + 0.7) (3 + 5) \times 10 = 96 \text{ N}$

71.
$$\frac{1}{2}$$
mv_A² + 0 = $\frac{1}{2}$ mv_B² + mg(2 ℓ)



If
$$v_B = v$$
 then $v_A = 2v$ (given)

$$\therefore \frac{1}{2}m(2v)^2 = \frac{1}{2}mv^2 + 2mg\ell$$
$$\frac{1}{2}mv^2 \times 3 = 2mg\ell$$

$$v=2\sqrt{\frac{g\ell}{3}}$$

72.
$$F = \frac{d(mv)}{dt} = v \frac{dm}{dt}$$
$$= 0.2 \times 2 = 0.4 \text{ kg-m/s}$$

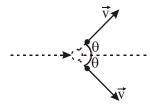
Power (P) =
$$\frac{\text{Work}}{\text{Time}}$$

$$= \frac{\text{Force} \times \text{Displacement}}{\text{Time}} = \text{Force} \times \text{velocity}$$

$$= 0.4 \times 0.2 = 0.08$$
 J/s or watt

73. Initial horizontal momentum = Final horizontal momentum

 $2kg\times4/m/s = 1kg\times v \cos\theta m/s+1 kg\times v \cos\theta m/s$



$$8 = 2v \cos \theta$$

$$v \cos \theta = 4 \text{ m/s} \qquad \dots (i)$$

The initial kinetic energy of the shell

$$= \frac{1}{2} \times 2kg \times (4m/s)^2$$
$$= 16 J$$

An amount of 48 J is imparted by explosion. Thus, the total energy of the fragments is 64 J, i.e. each fragment has 32 J kinetic energy.

$$= \frac{1}{2} \times 1 \text{kg} \times \text{v}^2 = 32 \text{J}$$

$$v^2 = 64$$

$$v = 8 \text{ m/s}$$

and
$$v \cos \theta = 4$$

$$\cos \theta = \frac{1}{2} \Rightarrow \theta = 60^{\circ}$$

74.
$$s = 6t^3 - t^2 - 1$$

$$v = \frac{ds}{dt} = 18t^2 - 2t$$

At
$$t = 0; v = 0$$

At
$$t = 3s$$
; $v = 18 \times 9 - 2 \times 3 = 156$ m/s

Also
$$W = \frac{1}{2}m(v_2^2 - v_1^2)$$

$$= \frac{1}{2} \times 3(156^2 - 0)$$

$$= 36504 J$$

75. Let the spring constant of spring Q is k and that of P is 2k. The extensions produced by applying equal forces on them are x_p and x_Q , respectively. Since F = kx (numerically)

or
$$x = \frac{F}{k}$$

and
$$U = \frac{1}{2}kx^2$$

or
$$U = \frac{1}{2}k\left(\frac{F}{k}\right)^2 = \frac{F^2}{2k}$$

or
$$U \propto \frac{1}{k}$$

Thus,
$$\frac{U_Q}{U_P} = \frac{k_P}{k_Q} = \frac{2k}{k} = 2$$

or
$$U_Q = 2U_P = 2E$$

76.
$$e = \frac{\text{Relative velocity after collision}}{\text{Relative velocity before collision}}$$

For the collision between the blocks A and B

$$e = \frac{v_B - v_A}{v_A - v_B} = \frac{v_B - v_A}{10 - 0} = 0.5$$

$$(\because u_{B} = 0 \text{ and } u_{A} = 10 \text{ m/s})$$
 or
$$v_{B} - v_{A} = 5 \qquad(i)$$

Also from the principle of conservation of linear momentum,

$$mu_A + mu_B = mv_A + mv_B$$
 or
$$10 + 0 = v_A + v_B$$
 or
$$v_B + v_A = 10$$
(ii)

From eqs. (i) and (ii)

$$v_B = 7.5$$
 m/s and $v_A = 2.5$ m/s

Now for the collision between the blocks B and C.

$$e = \frac{v_C - v_B}{u_B - u_C} = \frac{v_C - v_B}{7.5 - 0} = 0.5$$

or
$$v_C - v_B = 7.5 \times 0.5 = 3.75$$
 ...(iii)

and also from momentum conservation principle,

$$mu_B + mu_C = mv_B + mv_C$$
$$7.5 + 0 = v_B + v_C$$

or
$$v_C + v_B = 7.5$$
 ...(iv)

From eqs. (iii) and (iv), we get

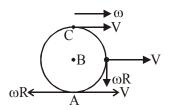
$$v_{\rm C} = 5.6 \text{ m/s}$$

77.
$$\overrightarrow{V}_A = V\hat{i} + \omega R(-\hat{i}); \overrightarrow{V}_B = V\hat{i}; \overrightarrow{V}_C = V\hat{i} + \omega R\hat{i}$$

$$\vec{V}_C - \vec{V}_A = 2\omega R\hat{i}$$

$$2[\overrightarrow{V}_A - \overrightarrow{V}_C] = 2[V(i) - V(i) - \omega R(i)] = -2\omega R(i)$$

Hence
$$\vec{V}_C - \vec{V}_A = -2(\vec{V}_B - \vec{V}_C)$$



78. Angular momentum of a body of mass m moving with velocity v in circular orbit of radius r about the centre of the orbit is = mvr

From the angular momentum conservation principle, if v' is the linear velocity of the coment when it is farthest distance r' from the sun, then

$$mv' r' = mvr$$

$$v' = \frac{vr}{r'} = \frac{6 \times 10^4 \times 8 \times 10^{10}}{1.6 \times 10^{12}} = 3 \times 10^3 \,\text{m/s}$$
$$\tau = F. \, r_{\perp}$$
$$= F. \, R$$
$$\tau = I\alpha$$

where
$$I = \frac{1}{2}MR^2$$

(Moment of inertia of the disc about axis passing through its centre and \bot to its plane face)

$$\therefore \qquad I\alpha = F. R$$

$$\alpha = \frac{FR}{I} = \frac{F.R}{\frac{1}{2}MR^2} = \frac{2F}{MR}$$

Thus, $\alpha \propto \frac{1}{R}$